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COMBINED FORWARD-FLYBACK-CONVERTER WITH ONLY TWO DIODES – FUNCTION AND MODELLING

A combined forward and flyback converter with a simple two windings transformer, an inductor, an active switch, two diodes and a buffer capacitor is explained. The voltage transfer ratio and the demagnetizing condition are derived. The voltage transfer ratio of the new converter is significantly higher compared to the forward and the flyback converters. The converter is useful for applications where a flyback converter is too small and a forward converter with its complicate transformer is too expensive. By shunting the two diodes by a third one the efficiency can be increased and due to the reduced losses the cooling is easier. The state space equations of the different states of the converter are derived.

1. Introduction

The well-known classical forward converter [1, 2, 3, 4, 5] needs three windings. Two are used to transform the energy and the third one is necessary to demagnetize the core. The new combined forward-flyback converter (Fig. 1) needs only two windings [6]. The transformer is therefore easier to manufacture, is smaller, has lower weight and is therefore cheaper. No additional component compared to the classical forward converter is necessary. Some other concepts for forward converters are published [7, 8, 9, 10, 11, 12 and 13].

Fig. 1 Circuit of the combined forward-flyback converter

2. Function

To explain the principal function, the following assumptions are made: ideal devices, discontinuous inductor current mode (DICM), the circuit is in steady state condition, the output capacitor is so large that the output voltage is constant, and the input of the circuit

is fed by a constant voltage source. The switching period can be divided into three states (Fig. 2).

A. State 1

The circuit diagram of state 1 is shown in Fig 2a. The active switch S is closed. The input voltage is applied to the primary winding N_1 and the input current rises linearly (dot and dash line). The voltage $(N_2/N_1)V_1$ is now across the secondary winding N_2 . The secondary current now closes over the diode D_1 , the output inductor L , and the secondary winding N_2 (dotted line). The current rises linearly according to

$$\frac{di_{N2}}{dt} = \frac{N_2}{N_1} \cdot \frac{V_1}{L} \quad (1)$$

The load is supplied by the capacitor C (long dashed line). The input current consists of two components: the transformed secondary current and the current to magnetize the transformer (primary inductance which has N_1 turns)

$$i_{N1} = \left[\left(\frac{N_2}{N_1} \right)^2 \cdot \frac{V_1}{L} + \frac{V_1}{L_1} \right] \cdot t \quad (2)$$

Fig. 2a State 1 of the combined forward-flyback converter

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B. State 2

The circuit diagram of state 2 is shown in Fig 2b. The active switch S is turned off. As the magnetic fluxes have to be steady, two new current loops start to function. The current through the storage inductor L closes via capacitor C and the diodes D_1 and D_2 (short dash line). The magnetizing current commutates from winding N_1 into winding N_2 and closes via capacitor C and the diode D_2 (dotted line). The value of the magnetizing current in N_2 jumps at this moment to

$$i_{N_2} = \frac{N_1}{N_2} \frac{V_1}{L_1} t_1 \quad (3)$$

and increases according

$$\frac{di_{N_2}}{dt} = -\frac{V_2}{L_1} \cdot \left(\frac{N_1}{N_2}\right)^2 \quad (4)$$

until the current reaches zero and the transformer is demagnetized (cf. Fig. 3b). As in state 1 the load is parallel to the capacitor C (long dashed line). To avoid the loss caused by the series connection of the two diodes, a third diode in forward direction between the anode of the second diode D_2 and the cathode of the first diode D_1 has to be connected.

Fig. 2b State 2 of the combined forward-flyback converter

C. State 3

The circuit diagram of state 3 is shown in Fig. 2c. Both the transformer and the storage inductor are demagnetized. The load is supplied by capacitor C (long dashed line). Stage three ends when S is turned on again. The circuit is now in state 1 again.

Fig. 2c State 3 of the combined forward-flyback converter

3. Voltage Transfer Rate

A. Combined forward-flyback converter

To calculate the voltage transfer rate of the combined forward-flyback converter, the assumption is used that the output power must be the same as the input power when ideal components are used

$$P_{out} = \frac{V_2^2}{R} = P_m \quad (5)$$

The current in the inductor L (Fig. 3.a) rises during the on-time of the switch S according to

$$\Delta I_L = \frac{V_1}{L} \cdot \frac{N_2}{N_1} \cdot d \cdot T \quad (6)$$

and leads to a stored energy at the end of the on-time of the active switch of

$$W_L = \frac{\Delta I_L^2}{2} \cdot L \quad (7)$$

The magnetizing energy of the transformer increases with the magnetizing current, which reaches

$$\Delta I_m = \frac{V_1}{L_1} \cdot d \cdot T \quad (8)$$

at the end of the turn-on time of the active switch leading to

$$W_m = \frac{\Delta I_m^2}{2} \cdot L_1 \quad (9)$$

During the off-time of the active switch this energy has to be decreased to zero, so that both inductive components are demagnetized again. Within one second the absorbed power of the converter is

$$\frac{V_2^2}{R} = f \cdot (W_L + W_m) \quad (10)$$

The output voltage can now be calculated according to

$$V_2 = \sqrt{R} \cdot \frac{V_1 \cdot d}{\sqrt{2} \cdot f} \cdot \sqrt{\left(\frac{N_2}{N_1}\right)^2 \cdot \frac{1}{L} + \frac{1}{L_1}} = K_C \cdot \sqrt{R} \cdot V_1 \cdot d \quad (11)$$

with K_C as a constant consisting of the converter parameters inductor L , magnetizing (primary) inductance L_1 , winding ratio N_2/N_1 , and switching frequency f .

To compare the combined converter with the conventional forward and the conventional flyback converter, we have to calculate the output voltage in the discontinuous mode. The discontinuous mode is necessary to demagnetize the inductive devices completely.

Fig. 3a Current through the inductor L

The transformer has to be demagnetized before the active switch is turned on again.

Fig. 3b Current through the secondary winding N_2

Duty cycle requirement

The converter has to be operated in the discontinuous mode. The maximum current through the inductor is

$$\Delta I_L = V_1 \cdot \frac{N_2}{N_1} \cdot \frac{d \cdot T}{L} \quad (12)$$

and the time that is needed for demagnetizing this coil is

$$T_{DL} = \frac{L \cdot \Delta I_L}{V_2} = d \cdot T \cdot \frac{V_1}{V_2} \cdot \frac{N_2}{N_1} \quad (13)$$

It must be valid

$$d \cdot T + T_{DL} < T \quad (14)$$

and therefore we get the constraint

$$d \cdot \left(1 + \frac{V_1}{V_2} \cdot \frac{N_2}{N_1} \right) < 1. \quad (15)$$

The transformer has to be demagnetized completely. The maximum magnetizing current (8) on the primary side has to be converted by the winding ratio to the secondary side. The necessary demagnetization time of the converter is now

$$T_{DT} = \frac{V_1}{V_2} \cdot d \cdot T \cdot \frac{N_2}{N_1} \quad (16)$$

It must be valid

$$d \cdot T + T_{DT} < T \quad (17)$$

and therefore we get again the constraint

$$d \cdot \left(1 + \frac{V_1}{V_2} \cdot \frac{N_2}{N_1} \right) < 1. \quad (18)$$

The demagnetizing time is the same for the inductor and the transformer.

With (11) and (18) we can write

$$d < 1 - \frac{N_2}{N_1} \cdot \frac{1}{K_c \cdot \sqrt{R}} \quad (19)$$

with converter coefficient

$$K_c = \sqrt{\left[\left(\frac{N_2}{N_1} \right)^2 \cdot \frac{1}{L} + \frac{1}{L_1} \right] \cdot \frac{1}{2 \cdot f}} \quad (20)$$

B. Forward converter

To calculate the output voltage of the forward converter (Fig. 4), only the energy in the inductor has to be taken into consideration, the magnetizing energy of the transformer is fed-back to the input voltage source via the additional winding N_3 . The maximum stored energy depends on the maximum inductor current which is reached at the end of the on-interval of the active switch

$$\Delta I_L = \left(\frac{N_2}{N_1} \cdot V_1 - V_2 \right) \cdot \frac{1}{L} \cdot d \cdot T. \quad (21)$$

Within the time

$$\Delta T = L \cdot \Delta I_L \cdot \frac{1}{V_2} = \left(\frac{N_2}{N_1} \cdot V_1 - V_2 \right) \cdot \frac{d \cdot T}{V_2} \quad (22)$$

the inductor is discharged. The mean value of the inductor current must be the same as the load current.

The input power of the converter is the input voltage multiplied by the mean value of the input current. The input current is triangular in shape. The input power is therefore

$$P_{in} = V_1 \cdot \frac{1}{T} \cdot \frac{1}{2} \cdot \frac{N_2}{N_1} \cdot \left(\frac{N_2}{N_1} \cdot V_1 - V_2 \right) \cdot \frac{1}{L} \cdot d^2 \cdot T^2 \quad (23)$$

and this must be equal to the output power

$$P_{out} = \frac{V_2^2}{R} = V_1 \cdot I_1 = P_{in}. \quad (24)$$

The output voltage of the forward converter in discontinuous mode can now be evaluated according to

$$V_2 = \frac{N_2}{N_1} \cdot \frac{R \cdot V_1 \cdot d^2}{4 \cdot L \cdot f} \cdot \left(-1 + \sqrt{1 + \frac{8 \cdot L \cdot f}{R \cdot d^2}} \right). \quad (25)$$

Fig. 4 Circuit of the classical forward converter

C. Flyback converter

The circuit diagram of the flyback converter is shown in Fig 5. Under the assumption of ideal components the output power must be the same as the input power

$$P_{out} = \frac{V_2^2}{R} = P_{in} . \quad (26)$$

Fig. 5 Circuit of the classical flyback converter

The magnetizing energy of the transformer increases with the magnetizing current, which reaches

$$\Delta I_m = \frac{V_1}{L} \cdot d \cdot T \quad (27)$$

at the end of the turn-on time of the active switch leading to.

$$W_m = \frac{\Delta I_m^2}{2} \cdot L_1 \quad (28)$$

$$\frac{V_2^2}{R} = f \cdot W_m . \quad (29)$$

The output voltage can now be calculated according to

$$V_2 = \sqrt{\frac{1}{2 \cdot f \cdot L_1}} \cdot \sqrt{R} \cdot V_1 \cdot d = K_F \cdot \sqrt{R} \cdot V_1 \cdot d , \quad (30)$$

with K_F as a constant consisting of the magnetizing inductance L_1 , and the switching frequency f .

4. Theoretical Results

The voltage transfer ratio of the three converters is compared for the same different load resistances, constant input voltage, and the same component values for all three topologies $L_1 = L_3 = 300 \mu\text{H}$, $L_2 = 75 \mu\text{H}$, $L = 50 \mu\text{H}$.

The scales are the same for all diagrams. Fig. 6a shows the voltage transfer ratio of the combined forward-flyback converter and Figs. 6b and 6c show the voltage transfer rate for the forward and the flyback converter, respectively. The voltage transfer ratio of the new converter is significantly higher compared to the forward and the flyback converters.

5. Statespace Description of the Combined Converter

The state variables are the flux ϕ of the transformer, the inductor current i_L , and the capacitor voltage u_C . The input variable is the input voltage u_1 . The fixed forward voltage of the diodes (the

Fig. 6a Voltage transfer ratio of the combined forward-flyback converter

Fig. 6b Voltage transfer ratio of the classical forward converter

Fig. 6c Voltage transfer ratio of the classical flyback converter

diodes are modeled as fixed forward voltages V_{D1} , V_{D2} and additional voltage drops depending on the differential resistors of the diodes R_{D1} , R_{D2}) are included as additional vectors. The parasitic

resistances are the on-resistance of the active switch R_S , the series resistance of the coil R_L , the series resistor of the capacitor R_C , and the differential resistors of the diodes R_{D1} , R_{D2} . With the A_L value of the transformer material the primary inductor is $L_1 = A_L \cdot N_1^2$ and the secondary inductor is $L_2 = A_L \cdot N_2^2$. The abbreviation $R_C//R$ describes the parallel connection of the series resistor of the output capacitor and the load resistor.

In discontinuous inductor current mode there are three states. In state one the active switch is turned on and also the passive switch D_1 turns on. Fig. 7a shows this switching state one. There are other possibilities to analyze circuits with different methods like shown e.g. in [14]. This would be especially useful for calculating the spectrum for EMC analyses. The leakage inductor is not included. (The leakage inductor is small because of the bifilar winding and leads in practice to small reduction of the input voltage. The energy which is stored must be transformed into heat by a snubber circuit when the overvoltage across the active switch is too high.) The complete flux which is connected with the winding is $\psi = N \cdot \phi$.

Fig. 7a Equivalent circuit for stage one

The state space description is

$$\frac{d}{dt} \begin{pmatrix} \phi \\ i_L \\ v_C \end{pmatrix} = \begin{bmatrix} -\frac{R_{N1} + R_S}{L_1} & 0 & 0 \\ \frac{N_2}{L} \left(\frac{R_{N1} + R_S}{L_1} + \frac{R_{N2}}{L_2} \right) & -\frac{R_{D1} + R_L}{L} & 0 \\ 0 & 0 & -\frac{1}{C(R + R_C)} \end{bmatrix} \cdot \begin{pmatrix} \phi \\ i_L \\ v_C \end{pmatrix} + \begin{bmatrix} \frac{1}{N_1} \\ \frac{1}{L} \\ 0 \end{bmatrix} \cdot v_1 \begin{pmatrix} 0 \\ -\frac{1}{L} \\ 0 \end{pmatrix} \cdot V_{D1} \quad (31)$$

In state two the active switch S is turned off, the passive switch D_1 is still conducting, and the second passive switch D_2 turns on. Fig. 7b shows this switching state two. The state space description is

Fig. 7b Equivalent circuit for stage two

Fig. 7c Equivalent circuit for stage three

When the transformer and the coil are demagnetized the load current discharges the capacitor. Fig. 7c shows this switching state three. The change of the capacitor voltage is now

$$\frac{d}{dt} v_C = -\frac{v_C}{C(R + R_C)} \quad (33)$$

6. Measurement Results

Now some experimental results of the new converter topology will be shown. In Fig. 8 the voltage across the active switch (Ch2:

$$\frac{d}{dt} \begin{pmatrix} \phi \\ i_L \\ v_C \end{pmatrix} = \begin{bmatrix} \frac{R_C//R + R_{D2} + R_{N2}}{L_2} & -\frac{R_C//R + R_{D2}}{N_2} & -\frac{R}{N_2(R + R_C)} \\ -\frac{R_C//R + R_{D2}}{L \cdot L_2} & -\frac{R_C//R + R_{D1} + R_{D2} + R_L}{L} & -\frac{R}{L(R + R_C)} \\ \frac{R}{C(R + R_C)} & \frac{N_2 R}{CL_2(R + R_C)} & -\frac{1}{C(R + R_C)} \end{bmatrix} \cdot \begin{pmatrix} \phi \\ i_L \\ v_C \end{pmatrix} + \begin{bmatrix} 0 \\ \frac{1}{L} \\ 0 \end{bmatrix} \cdot V_{D1} \begin{pmatrix} -\frac{1}{N_2} \\ 0 \\ 0 \end{pmatrix} \cdot V_{D2} \quad (32)$$

20 V/div) and the current through the inductor (Ch1: 2 A/Div) can be seen. The results follow as predicted.

For more convenient measuring, a two-diode-combined-forward-flyback converter with a tapped inductor (autotransformer) was built (Fig. 9). The winding ratio is one to one and the windings are bifilar. The inductor L was realized with an isolated stranded wire and with a gapped core. No snubber was necessary because of the low leakage inductance of the autotransformer. The converter was used with open loop control.

Fig. 8 Current through the inductor (Ch1: 2 A/Div) and voltage across the active switch (Ch2: 20 V/div)

Fig. 9 Autotransformer two-diode-combined-forward-flyback converter

Figs. 10 and 11 show (up to down) the voltage across the active switch, the current through the inductor, and the current through the winding N_1 ; the input voltage is 24 V, the load is 11 Ohm and the duty cycle is 16% and 45% respectively. The output voltage is 14 V with the small duty cycle, and 38 V with the higher one.

The most interesting signal is the current through the autotransformer winding N_1 . During the on-time of the active switch, the current is the same as the one in the filter inductor. When the transistor turns off, the current of the inductor is freewheeling, and through N_1 now flows the magnetizing current of the autotransformer.

Fig. 10 Voltage across the active switch (Ch3: 20 V/div), current through the inductor (Ch1: 2 A/Div), and current through the winding N_1 (Ch2: 2 A/Div); input voltage 24 V, duty cycle 16%, output voltage 14 V, load 11 Ohm.

Fig. 11 Voltage across the active switch (Ch3: 20 V/div), current through the inductor (Ch1: 5 A/Div), and current through the winding N_1 (Ch2: 5 A/Div); input voltage 24 V, duty cycle 45%, output voltage 38 V, load 11 Ohm.

7. Conclusion

The combined forward-flyback converter with two diodes has three interesting aspects. Due to the fact that the voltage across the secondary winding N_2 and across the inductor L is the same, the converter must be used in the discontinuous mode. The transformer has to be demagnetized before the active switch is turned on again. This has the advantage that from the control point of view the converter is only a first order system, as all magnetic elements have no energy at the beginning of all switching periods. All diodes turn off naturally, no forced commutation occurs and this leads to reduced switching losses and a better efficiency. For the same values of the components more power can be transformed compared to the forward and flyback converter. A higher output voltage can be achieved by the same duty ratio compared to the forward and flyback converter. The converter is useful for applications where a flyback converter is too small (flyback converters have the disadvantage that for higher power ranges a big trans-

former has to be used) and a forward converter with its complicated transformer is too expensive. By shunting the two diodes by a third one, the efficiency can be increased and due to the reduced losses the cooling is easier. The converter is especially useful for renewable energy applications and for compact systems.

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