SIMULATION OF TORSION MOMENT AT THE WHEEL SET OF THE RAILWAY VEHICLE WITH THE TRACTION ELECTROMOTOR FOR WAVY DIRECT CURRENT

The phenomenon of mechanical resonance in the axial make of the railway vehicle with the traction electromotors for wavy direct current has been of topical interest for the railway connoisseurs for a long time. This is not randomly because mechanical resonance may cause crevices and fractures in the wheel set. Accordingly mechanical resonance may endanger safety of railway communication. However, previous research did not precisely investigate the influence of tension and current at the value and guise of torsion moment at the wheel set. Therefore, this paper defined adduced influence. Besides, this paper defined the optimal antislippage shield for all the railway vehicles with the traction electromotors for wavy direct current.

1. Introduction

Within the capital reparation of the diode ZS 441 series locomotives in 2006 and 2007, the modification of electric devices was realised. The modification of the diode ZS 441 series locomotives was realised at the electric devices because the Directorate of "Serbian Railway" wanted a greater reliability in service and better environment for the railway motorman. In the modification the high-tension tuner was ejected because the diode bridge was replaced with the half-conduct tiristore bridge. The traction circuit of the thyristor ZS 444 series locomotives was realised with two bimotor units. The first and the second bimotor unit comprised M1 and M3 and M2 and M4 traction electromotors for wavy direct current at the separate rotary socle. Accordingly, all wheel sets of the ZS 444 series locomotives have got the equal performance. Traction electromotors for wavy direct current in each bimotor unit are connected in a series – Fig. 1.

For the purpose of a precise analysis of the influence of wavy direct current on the value and guise of torsion moment at the wheel set we apply the operational method based on Laplace's transformation. This method will be described in the subsequent article.

2. Dynamics at the Wheel set of the Thyristor ZS 444 Series Locomotives

The propulsion system of the thyristor ZS 444 series locomotives is a mechanical system which comprises the traction electromotor for wavy direct current (3), a cogged clamp (2), a cardan shaft (5), a rubber clamp, a reductor (1), the driving shaft (4) and a monoblock wheel (Fig. 2) [1, 2].

The essential running of the mechanical system is a rotation with a transfer of operative moment from the shaft of the traction electromotor to the monoblock wheel. Researches have shown that the described mechanical system may generate a strong torsion oscillation and fracture of the wheel set [1, 2].
The dynamic balance of the shaft of the traction electromotor for wavy direct current is described by the next equation [1, 2, 3]:

\[ J_m \frac{d\omega}{dt} = M - M_v \]  

(1)

where \( J_m \) is the inertial moment of rotating mass with the angular speediness \( \omega \). The inertial moment \( J_m \) is a sum of inertial moment of the traction electromotor for wavy direct current (550 Nms\(^2\)), inertial moment of the cogged clamp (2 Nms\(^2\)), inertial moment of the cardan shaft (3 Nms\(^2\)), inertial moment of the rubber clamp (10 Nms\(^2\)) and inertial moment of the lesser gear of the jagged reductor (10 Nms\(^2\)). Therefore, the inertial moment is \( J_m = \frac{575}{H_{11005}} \) Nms\(^2\) [3]; \( \omega \) – angular speediness of the shaft of the traction electromotor for wavy direct current; \( M(t) \) – transient value of torque at the shaft of the traction electromotor for wavy direct current; \( M_v(t) \) – transient value of torque oncoming from idler force; \( D \) – diameter of the monoblock wheel (\( D = 1210 \) mm); \( i \) – transfer ratio of the jagged reductor (\( i = 3.65 \)).

Fig. 3 shows the courses of the operative moment \( M_0 \) and the torque \( M_v \) of the reaction force

\[ \vec{F}_v(\vec{F}_v = -\vec{F}_o) \]. \( J_0 \) in Fig. 3 denominates the inertial moment of rotating mass with the angular speediness \( \omega_0 \). The inertial moment \( J_0 \) is the sum of inertial moment of the larger gear of the jagged reductor (180 Nms\(^2\)); inertial moment of the driving shaft (340 Nms\(^2\)) and inertial moment of the monoblock wheel (1600 Nms\(^2\)). The total inertial moment is \( J_0 = \frac{2120}{H_{11005}} \) Nms\(^2\) [3].

The equation of dynamic balance for the shown system in Fig. 3 is:

\[ J_m \frac{d\omega}{dt} = M_i - M_v \]  

(2)

where

\[ \omega_0 = \frac{2}{D} \quad \eta = \frac{\omega_0}{i} \]  

(3)

\[ M_i = \eta \cdot i \cdot M_v \]  

(4)

\[ M_v = \frac{D}{2} \cdot F_v \]  

(5)

\[ \eta = 0.975 \text{ (grade of utility according to the IEC - 349)} \]

Based on equations (1) and (4):

\[ J_m \frac{d\omega}{dt} = \frac{M_i}{\omega_0}(M_0 - M_i) \]  

(6)

where \( M_0 = \eta \cdot i \cdot M_v = 27924.8849 \) Nm

Based on equations (2) and (5):

\[ J_m \frac{d\omega}{dt} = M_v - \frac{D}{2} \cdot F_v \]  

(7)

The equation of the mechanical system running is:

\[ m \frac{dv}{dt} = F_v - \Sigma F_v \]  

(8)

where: \( m \) – mass of each wheel set; \( \Sigma F_v \) – total reaction forces (\( \Sigma F_v \) is the sum of friction force of the wheel-rail system; friction force in a shaft bolster; friction force of air; reaction force on a slope; reaction force on a curvature and reaction force of inertia of locomotive.

Based on the former equations:

\[ \left( J_0 + m \left( \frac{D^2}{2} \right) \right) \frac{d\omega_0}{dt} - \frac{M_v}{\omega_0} (M_0 - M_v) = \frac{D}{2} \Sigma F_v \]  

(9)

where: \( \omega_0 = \frac{\omega_0}{i} = 35.8438 \) \( \frac{rad}{s} \); \( M_0 = \frac{D}{2} \Sigma F_v \) – comparative value of the reaction momentum.

Based on the equations (6) and (9), the angular speedinesses \( \omega \) and \( \omega_0 \) have got forms in the complex domain:

\[ \omega = \frac{M_i (M_0 - M_v)}{J_0 \cdot \omega_0 \cdot s} \]  

(10)

\[ \omega_0 = \frac{M_0 (M_0 - M_v)}{\left( J_0 + m \left( \frac{D^2}{2} \right) \right) \omega_0 \cdot s} \]  

(11)

The torsion moment of the driving shaft (4) – Fig. 2:
\[ M = k \cdot \Delta \theta \]  
(12)

\[ \Delta \theta = \frac{1}{i} \theta - \theta_0 \]  
(13)

\[ \omega_n = \frac{d\theta_n}{dt}, \text{in the complex domain} \quad \theta_n = \frac{\omega_n}{s} \]  
(14)

\[ \omega = \frac{d\theta}{dt}, \text{in the complex domain} \quad \theta = \frac{\omega}{s} \]  
(15)

where \( k \) – torsion constant of driving shaft (4) – Fig. 2. The torsion constant of the leaves part of the driving shaft (i.e. part of the driving shaft from the jagged reductor to the near monoblock wheel) is \( k_1 = 553 \cdot 10^5 \text{Nm rad}^{-1} \). Torsion constant of the longer part of the driving shaft (i.e. part of the driving shaft from the jagged reductor to the further monoblock wheel) is \( k_2 = 9.8 \cdot 10^6 \text{Nm rad}^{-1} \) [3]; \( \theta_0 \) – banking of driving shaft (4) induced by the wheel-rail system.

3. Resonance Frequency of the wheel set

As

\[ \theta_n = \frac{k}{i \left( J_0 + m \left( \frac{D}{2} \right)^2 \right) \cdot s^2 + k} \]  
(16)

Transfer function \( W_m \) is:

\[ W_m = \frac{M}{M} = \frac{1}{J_0 \cdot k + \frac{k}{\eta \cdot i} \left( J_0 + m \left( \frac{D}{2} \right)^2 \right) \cdot s^2} \]  
(17)

\[ \omega = \frac{\sqrt{J_0 \cdot k + \frac{k}{\eta \cdot i} \left( J_0 + m \left( \frac{D}{2} \right)^2 \right)}}{J_0 \left( J_0 + m \left( \frac{D}{2} \right)^2 \right)} \]  
(18)

Based on the equation (18), resonance frequencies of the leaves and longer of the driving shaft (4) – Fig. 2 are:

\[ \omega_1 = 526.87 \text{ rad s}^{-1} \]  
(19)

\[ \omega_2 = 70.14 \text{ rad s}^{-1} \]  
(20)

4. Torsion moment at a Slippage of the Wheel set

Based on the former equations, we made a program in MATLAB-SIMULINK to simulate the torsion moment at the wheel set. We received a chronological variety of the torsion moment of the longer part of the driving shaft according to Fig. 4 when we started from this simulation program. We assumed that a slippage of the wheel set appeared because of a nuisance value of the traction coefficient at \( M_{m_r} = \frac{D}{2} \Sigma F_n \) = 1 (The traction coefficient at this environment is defined by the following term: \( F_t > \mu \cdot Q \rightarrow \mu < \frac{M_{m_r}}{D} \cdot Q \cdot \frac{1.21}{2} \cdot 200000 \)).

We also assumed that the rotating moment of the shaft of the traction electromotor for wavy direct current is determined by:

\[ M(t) = \frac{33}{32} \cdot k \cdot J_0 \left( 1 + \frac{16}{33} \cos 2\omega t + \frac{1}{33} \cos 4\omega t \right) = M_0 \left( 1 + a_1 \cos 2\omega t + a_2 \cos 4\omega t \right) \]  
(21)

where \( M_0 \) – in between value of the torque of the shaft of the traction electromotor for wavy direct current; \( a_1 = 16/33 \) – factor amplitude of a frequency 2f = 2 \cdot 50 = 100 Hz; \( a_2 = 1/33 \) – factor amplitude of a frequency 4f = 4 \cdot 50 = 200 Hz.

![Fig 4 Comparative value of the torsion moment of the longer part of the driving shaft at a frequency during 2f = 2 \cdot 50 = 100 Hz the slippage of the wheel set](image-url)
Based on Fig. 4, we can conclude that the torsion moment of the longer part of the driving shaft quite quickly rises during the slippage of the wheel set. This moment achieved the value of $M_{t1c}/M_{ts} = 23$ ($M_{t1} = 6.42$ MNm) in a quite short period of $t \leq 0.3$ s. Consequently, the torsion moment during the slippage of the wheel set will permanently impair the longer part of the driving shaft.

If we curtail the value of the factor amplitude of a frequency $2f = 2 \cdot 50 = 100$ Hz from $a_1 = 16/33$ to $a_1 = 0.1$, the dependence $M_{t1c}/M_{ts} = f(t)$ during the slippage of the wheel set will be according to Fig. 5. (The factor amplitude $a_1$ may dwindle if we enlarge inductance of central silencer).

Based on Fig. 5, we can conclude that the torsion moment at $a_1 = 16/33$ is five times smaller than the torsion moment $a_1 = 0.1$ at during the slippage of the driving wheel set. The peak value of the torsion moment of the longer part of the driving shaft at $a_1 = 0.1$ is attained in $t = 0.25$ s. Besides, our program for simulation showed that the peak value of this moment further dwindled while we were further dwindling the factor amplitude of a circular frequency $2f = 2 \cdot 50 = 100$ Hz.

If we commute the diode or asymmetrical thyristor rectifier with the symmetrical thyristor rectifier, we’ll receive a passable value of the torsion moment with the frequency $2f = 2 \cdot 25 = 50$ Hz. The dependence $M_{t1c}/M_{ts} = f(t)$ during the slippage of the wheel set with the frequency $2f = 2 \cdot 25 = 50$ Hz and $a_1 = 3$ is shown in Fig. 6.

Based on Fig. 6, we can conclude that the substitution of the diode rectifier or the asymmetrical with modern symmetrical thyristor rectifier relates to a passable value of the torsion moment during the slippage of the wheel set. Besides, this substitution will eject the cascade switch and simplify the traction transformer. This substitute may also enable the application of recuperative brake. Consequently, we believe that the modern symmetrical thyristor rectifier may eliminate the impairing of the longer part of the driving shaft during the slippage. With this rectifier the existing antislippage shield of the ZS 441, ZS 461 and ZS 444 electrolocomotives will be enough speedy though now it is not.

5. Conclusion

The torsion moment of the longer part of the driving shaft rises quite quickly during the slippage of the wheel set. This moment was achieving the value of $M_{t1c}/M_{ts} = 23$ ($M_{t1} = 6.42$ MNm) in quite a short period of $t \leq 0.3$ s. Consequently, torsion moment during the slippage of the wheel set will permanently impair the longer part of the driving shaft.

The torsion moment of the longer part of the driving shaft at $a_1 = 16/33$ is five times smaller than the torsion moment at $a_1 = 0.1$ during the slippage of the wheel set. The peak value of the torsion moment of the longer part of the driving shaft at $a_1 = 0.1$ is attained in $t = 0.25$ s. Besides, our program for simulation showed that the peak value of this moment further dwindled while we were further dwindling the factor amplitude of a frequency $2f = 2 \cdot 50 = 100$ Hz.

The substitution of the diode rectifier or the asymmetrical with modern symmetrical thyristor rectifier relates to a passable value of the torsion moment with the frequency $2f = 2 \cdot 25 = 50$ Hz during the slippage of the wheel set. Besides, this substitution will eject the cascade switch and simplify the traction transformer. This substitution may also enable the application of recuperative brake. Consequently, we believe that the modern symmetrical thyristor rectifier may eliminate the impairing of the longer part of the driving shaft during the slippage.
References


