1. Introduction

This article describes the authors’ own mathematical modelling for the production process of a new type of low-weight composite frame. A new type of low-weight composite frame of high quality is used for example in the transport industry [1, 2 and 3]. Reasons for the use of composites not only in transport industry (car industry, aerospace industry, aeronautic industry, etc.) are derived from the current requirements for the low-weight parts. The construction of composite frames must be light because, for example, in car industry an optimal weight and power usage lead to emission reductions. But concurrently the construction of design parts must be sufficiently solid and rigid. We will describe technology of carbon or glass filament rovings wound around the polyurethane core which is a frame shape in 3D with a varying shape and size of cross-section of the frame. In the following part of the article we will consider only a circular cross-section. If the frame cross-section is not circular, we consider an imaginary cylindrical “envelope” (with minimum possible radius) stretched on the frame surface. Traditional procedures of composite manufacturing are labour-intensive and time-consuming. Moreover, the traditional techniques do not ensure accurate fibre winding around the core. The use of industrial robots in composite production greatly reduces production costs, production time and minimises scrap rate. Other problems of industrial robot trajectory are also solved in publications, e.g. [4 - 7]. Composites offer an attractive material properties-to-production cost ratio. One of the possible methods for producing composites is to stretch the fabric from the fibres on a core with an arbitrary geometry. However, if the core of the composite is a 3D frame or a frame with a very complicated 3D shape or several layers of the fibre strands are wound simultaneously around the core, then this method is not suitable. In such cases, the method of dry winding of endless fibre strands around a core geometry using a rotary fibre-processing head is often used for the composite production. This method provides full control over the placement, laying direction, and the amount of fibres on the core as well as the homogeneity of the structure. The final composite is obtained after dry winding of the required layers of strands around the core by injection of the resin to the mould using heat and pressure. Now, we are describing the process of producing composites with a polyurethane core of...
end-effector. The passage of the core through the fibre-processing head is controlled by the movement of the robot-end-effector. When polyurethane core passes through fibre-processing head the strands are successively wound on the surface of the core at a targeted angle. First, the outer rotating guide line ensures winding strands under the angle 45° (relative to the axis of the head and the moving direction of the core). Subsequently, the middle static guide winds the second layer of strand under the angle 0° and the second outer rotation winds the final layer of strands 45°. Our goal is for the core to pass through the fibre-processing head orthogonal to the guide lines of the head as far as possible. The principle of the winding solution is shown in Fig. 2 (fibre processing head contains only one rotation line in this figure). To optimise the manufacturing process we made a numerical model for calculating the robot-end-effector trajectory to achieve an optimal directional orientation of the fibre placement in the manufacture of the composite frame profile. The mathematical calculation of trajectory was programmed in the Delphi development environment. This article describes a numerical model for quality of the manufacturing process technology of a shaped composite in 3D space. As already mentioned, providing the correct angles for winding of strands around the core is mainly conditioned by the determination of the appropriate trajectory of the robot-end-effector. Orthogonal direction of passage of the core (of a closed frame shape) to the guide line in the place of its own winding of fibres around the core surface ensures the correct angle and uniformity of winding. The quality of fibre winding also depends on the material properties of polyurethane core and fibres (especially on adhesion of the fibre to the core).

2. Numerical model describing the fibre winding process for a composite frame

This chapter briefly describes the numerical model of the optimal process of winding strands around a 3D polyurethane core with a circular cross-section. The core shape is a frame and the radius of the circular cross section of the frame may be generally different for individual parts of a frame. The actual process of strand winding is carried out using a fibre-processing head and an industrial robot. The polyurethane core is attached to the robot-end-effector and the winding head is fixed in the workspace of the robot. Within the described numerical model (Fig. 3), we will consider the right-handed Euclidean coordinate system $E_3$ of the robot ($BCS$). We will describe the positions of the individual parts of an experimental workplace of winding strands to frame using this coordinate system. Subsequently, we will consider the local right-handed Euclidean coordinate system of the robot-end-effector ($LCS$). To avoid any misunderstanding, we will label the points and vectors with coordinates in $BCS$ with the subscript $BCS$ and points and vectors with coordinates in $LCS$ with the subscript $LCS$. The fibre-processing head is fixedly placed in the workspace of the robot and coordinates of its parts are specified in the basic coordinate system of the robot. The used fibre-processing head contains three guide lines (Fig. 2). Each guide line contains twelve fixed fibre coils along its periphery. The outer guidelines rotate around a common axis and the intermediate guideline is static. The polyurethane core of a frame shape is attached to the robot-end-effector. The passage of the core through the fibre-processing head is controlled by the movement of the robot-end-effector. When polyurethane core passes through fibre-processing head the strands are successively wound on the surface of the core at a targeted angle. First, the outer rotating guide line ensures winding strands under the angle 45° (relative to the axis of the head and the moving direction of the core). Subsequently, the middle static guide winds the second layer of strand under the angle 0° and the second outer rotation winds the final layer of strands 45°. Our goal is for the core to pass through the fibre-processing head orthogonal to the guide lines of the head as far as possible. The principle of the winding solution is shown in Fig. 2 (fibre processing head contains only one rotation line in this figure). To optimise the manufacturing process we made a numerical model for calculating the robot-end-effector trajectory to achieve an optimal directional orientation of the fibre placement in the manufacture of the composite frame profile. The mathematical calculation of trajectory was programmed in the Delphi development environment. This article describes a numerical model for quality of the manufacturing process technology of a shaped composite in 3D space. As already mentioned, providing the correct angles for winding of strands around the core is mainly conditioned by the determination of the appropriate trajectory of the robot-end-effector. Orthogonal direction of passage of the core (of a closed frame shape) to the guide line in the place of its own winding of fibres around the core surface ensures the correct angle and uniformity of winding. The quality of fibre winding also depends on the material properties of polyurethane core and fibres (especially on adhesion of the fibre to the core).
LCS with the subscript LCS. Activities of the industrial robot are controlled using a robot control unit (in our case unit KR C4) and the library of instructions. For our purposes it is crucial to set the desired position of the robot-end-effector using the library of instructions. The position and orientation of the robot-end-effector is defined by using the LCS. The origin of the LCS is positioned in the robot-end-effector while at the same time the robot-end-effector is oriented in the direction of the positive part of the z-axis in the LCS with regard to the BCS. The actual position of the LCS with regard to the BCS is determined by the values listed in the "tool centre-point" (TCP). The tool centre point consists of six values TCP = (x, y, z, a, b, c). The first three parameters specify the coordinates of the origin of the LCS with regard to the BCS. The values a, b and c indicate the angle of the rotation of the LCS around the axes z, y and x with regard to the BCS. The non-bearing polyurethane frame can be described by the LCS - axis in the longitudinal direction, is static and so it is not necessary to calculate the passage of polyurethane frame through the fibre-processing head while the frame possibly rotates around the tangent of its axis o in point B[i]_LCS. In the following chapter we will describe the use of the mathematical model to calculate the trajectory of the robot-end-effector.

Fig. 3 Numerical model describing fibres winding process for a new composite frame

Fig. 4 Geometry of a polyurethane frame

Fig. 5 Points S1 and S2 lie on the axis s of the fibre-processing head
2.1 Mathematical model for calculating the trajectory of the robot-end-effector

In the derivation procedure of trajectory calculation, we used results listed in [1 and 7]. Note that the Denavit-Hartenberg method is often used to determine the trajectory of a robot (e.g. see [8]). In this chapter we will calculate such a trajectory of the robot-end-effector when the polyurethane frame attached to the robot-end-effector passes gradually through the fibre-processing head. Recall that the fibre-processing head and its parts are fixedly positioned in the BCS and a position of the polyurethane frame is defined in the LCS of the robot-end-effector. Determination of the trajectory is made on the basis of calculating the sequence of \( N \) of the TCP values, where \( 1 \leq i \leq N \). Then the robot-end-effector changes its position in relation to changes in parameters based on their linear interpolation (or the use of cubic splines) during the transition from the current TCP, \( T_{pi} \), to the subsequent TCP. Consequently, the frame passes through the fibre-processing head. The calculated parameters of the current TCP ensure that point \( B_i^{\text{BCS}} \) of the axis \( o \) of the frame will be the same as point \( H_{pi}^{\text{LCS}} \) (the middle of the fibre-processing head) in the \( i \)-th step of the polyurethane frame passing through the fibre-processing head. At the same time the vector \( \text{vector1}B_i^{\text{LCS}} \) of the tangent of the axis \( o \) of the frame at the point \( B_i^{\text{BCS}} \) identifies with the vector \( \text{vector1}H_{pi}^{\text{LCS}} \) (this vector indicates the direction of passage frame through fibre-winding head) and the vector \( \text{vector2}B_i^{\text{LCS}} \) identifies with the vector \( \text{vector2}H_{pi}^{\text{LCS}} \) (identification of this pair of vectors allows the polyurethane frame to turn around the tangent of the axis \( o \) in the point \( B_i^{\text{BCS}} \)). When the described identifications are complete (i.e. the two orthogonal vectors and their common starting point entered in the LCS are in the same position in BCS as the two orthogonal vectors and their common starting point in the BCS) the parameters of the corresponding TCP are unambiguously determined and, therefore, the position and orientation of the robot-end-effector relative to the LCS in the \( i \)-th step of passing the frame through the fibre-processing are also unambiguously determined. When calculating the sequence of the TCP values (1 \( \leq i \leq N \)) of the robot-end-effector, we use a matrix calculus to perform a transformation of the LCS of the robot-end-effector relative to the BCS. We will write points, vectors and matrices in a homogeneous form (i.e. point \( V = [x, y, z]^{\text{T}} \) vector \( u = (x, y, z, 1)^{\text{T}} \)) in the following text. We also use the Euclidean norm \( \|u\| = \sqrt{x^2 + y^2 + z^2} \) of vector \( u \), where \( \|u\| \). 

1. Calculation of the Passage of Frame Thorough the Fibre-processing Head

We calculate for \( i = 1, \ldots, N \) the TCP of the robot-end-effector so that at the same time \( B_i^{\text{LCS}}=H_{pi}^{\text{LCS}} \) vector1\( B_i^{\text{LCS}}=\text{vector1}\;H_{pi}^{\text{LCS}} \), vector2\( B_i^{\text{LCS}}=\text{vector2}\;H_{pi}^{\text{LCS}} \). After determining TCP\( i \), all of the TCP\( i \) parameters are continuously changed to the parameters of to the TCP. By this procedure we determine partial passage of the frame through the fibre-processing head. The initial TCP indicates the position and orientation of the robot-end-effector before the start of the passage of the frame through fibre-processing head. In the following section of this chapter we will focus on the procedure for determining TCP\( i \).

II. Determining the Transformation Matrix

We assume that TCP\( i = (x_i, y_i, z_i, a_i, b_i, c_i) \) is entered. With the aim of determining the transformation matrix \( T_{i} \) (which we will apply to LCS) in the form Eq. (1) we perform the following steps.

\[
T_i = L_i \cdot Q_i, \quad (1)
\]

i. We determine the coordinates of the vector \( \text{vector1}B_i^{\text{LCS}} \) in the coordinate system BCS (under the assumption that the coordinate systems BCS and LCS have the same origin, this assumption is used when finding the required rotation matrix). The matrix \( Q_{x_i} \) of the rotation LCS towards BCS is in the form of Eq. (2).

\[
Q_{x_i} = \text{Rot}(z, a_i) \cdot \text{Rot}(y, b_i) \cdot \text{Rot}(x, c_i).
\]

where \( \text{Rot}(z, a_i) \) is the orthogonal matrix of rotation of LCS around axis \( z \) at angle \( a_i \), \( \text{Rot}(y, b_i) \) orthogonal matrix of rotation of LCS around axis \( y \) at angle \( b_i \) and \( \text{Rot}(x, c_i) \) orthogonal matrix of rotation of LCS around axis \( x \) at angle \( c_i \).

\[
\text{Rot}(z, a_i) = \begin{bmatrix}
\cos a_i & -\sin a_i & 0 & 0 \\
\sin a_i & \cos a_i & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}
\]

\[
\text{Rot}(y, b_i) = \begin{bmatrix}
\cos b_i & 0 & \sin b_i & 0 \\
0 & 1 & 0 & 0 \\
-\sin b_i & 0 & \cos b_i & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}
\]

\[
\text{Rot}(x, c_i) = \begin{bmatrix}
\cos c_i & -\sin c_i & 0 & 0 \\
0 & \cos c_i & -\sin c_i & 0 \\
0 & \sin c_i & \cos c_i & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}
\]

Subsequently, we can express the coordinates of the vector \( \text{vector1}B_i^{\text{LCS}} \) in the BCS system in the form \( \text{vector1}B_i^{\text{LCS}} = Q_{x_i} \cdot \text{vector1}B_i^{\text{LCS}} \).

ii. By using the scalar product of vectors \( \text{vector1}H_{pi}^{\text{LCS}} \) and \( \text{vector1}B_i^{\text{LCS}} \) we determine their deviation \( \alpha \).

iii. We determine the cross product \( p_{\text{BKS}} = \text{vector1}H_{pi}^{\text{LCS}} \times \text{vector1}B_i^{\text{LCS}} \).

iv. Vector \( p_{\text{BKS}} \) is orthogonal to vectors \( \text{vector1}H_{pi}^{\text{LCS}} \) and \( \text{vector1}B_i^{\text{LCS}} \). We normalise vector \( p_{\text{BKS}} \) i.e., we ensure its unit length \( p_{\text{BKS}} \cdot p_{\text{BKS}} = 1 \). We perform the rotation of vector \( \text{vector1}B_i^{\text{LCS}} \) by angle \( \alpha \) around vector \( p_{\text{BKS}} \) (we consider the correct
orientation of angle \( \vec{v} \) by relation (8) will be valid \( \vec{H}_{\text{BCS}'} = \vec{H}_{\text{BCS}} \vec{B}_{\text{BCS}} \). Then \( \vec{L}_{\text{BCS}} = \vec{L}_{\text{BCS}} \vec{B}_{\text{BCS}} \).

If we denote \( \vec{p}_{\text{BCS}} = (\ell_{\text{BCS}}, s, n_s, a, 0)^T \), then the matrix \( \vec{R}(\vec{p}_{\text{BCS}}, \vec{\alpha}) \) will have the form (4), you can see in [1].

Where \( s \) and \( c \) indicate \( s = \sin \vec{\alpha}, c = \cos \vec{\alpha} \). At the same time we determine the vector \( \vec{l}_{\text{BCS}} \) (5).

The cases where \( \vec{\alpha} = 0 \) or \( \vec{\alpha} = \pi \) need to be solved separately.

v. By using the scalar product of the vectors, we determine the deviation \( \vec{b} \) of vectors \( \vec{v} \), \( \vec{H}_{\text{BCS}} \), and \( \vec{l}_{\text{BCS}} \).

vi. The resulting matrix of rotation \( \vec{Q} \) has the form of Eq. (6).

\[
\vec{Q} = \vec{R}(\vec{v} \cdot \vec{H}_{\text{BCS}}, \vec{b}) \cdot \vec{R}(\vec{p}_{\text{BCS}}, \vec{\alpha}) \cdot \vec{R}(\vec{z}, a) \cdot \vec{R}(\vec{x}, c, y) \cdot \vec{R}(\vec{y}, b, x) \cdot \vec{R}(\vec{z}, a_j)
\]

where the elements of the matrix \( \vec{R}(\vec{v} \cdot \vec{H}_{\text{BCS}}, \vec{b}) \) are analogously defined as elements of the matrix \( \vec{R}(\vec{p}_{\text{BCS}}, \vec{\alpha}) \) in relation (4). In relation (6) we use the correctly determined angle orientation of angle \( \vec{b} \) i.e. we rotate the vector \( \vec{l}_{\text{BCS}} \) (5) around the vector \( \vec{H}_{\text{BCS}} \) to the vector \( \vec{2H}_{\text{BCS}} \).

vii. The translation vector is defined (7) as

\[
\vec{u}(\vec{l}_{\text{BCS}}) = \vec{H}_{\text{BCS}} \vec{B}(\vec{l}_{\text{BCS}}) \cdot (x_{11}, y_{11}, z_{11}, 0)^T
\]

where matrix \( \vec{Q} \) is determined by the relation (6). We remember that \( x_{11}, y_{11}, z_{11} \) are the first three parameters of \( \text{TCP}_{\vec{4}} \). The resulting transformation matrix \( \vec{T}_r \) in the 4th step of the passing of the frame through the fibre-processing head is in the form (8).

\[
\vec{T}_r = \vec{R}(\vec{x}_{\text{ad}}, y_{\text{ad}}, z_{\text{ad}}) \cdot \vec{Q}_k
\]

where translation matrix

\[
\vec{R}(\vec{x}_{\text{ad}}, y_{\text{ad}}, z_{\text{ad}}) = \begin{bmatrix}
1 & 0 & 0 & x_{\text{ad}}
0 & 1 & 0 & y_{\text{ad}}
0 & 0 & 1 & z_{\text{ad}}
0 & 0 & 0 & 1
\end{bmatrix}
\]

and \( x_{\text{ad}}, y_{\text{ad}}, z_{\text{ad}} \) are components of vector \( \vec{u}(\vec{l}_{\text{BCS}}) \) in Equation (7).

After performing the LCS of the robot-end-effector the corresponding transformation matrix \( \vec{T}_r \) determined by relation (8) will be valid \( \vec{H}_{\text{BCS}} \vec{B}(\vec{l}_{\text{BCS}}) \vec{T}_r \vec{B}(\vec{l}_{\text{BCS}}) \).

III. Calculation of the Euler Angles

We will calculate the Euler angles. Any right-handed rotation in Euclidean space \( E_3 \) around the given unit vector \( \vec{p} \) by angle \( \vec{\varphi} \) is determined by the orthogonal matrix \( \vec{Q} = \vec{R}(\vec{p}, \vec{\varphi}) \), its elements are in the form (3) and det \( \vec{Q} = 1 \). Each rotation matrix can be written as a product of the matrices of rotation around the coordinate axes \( z, y \), and \( x \), i.e. \( \vec{Q} = \vec{R}(\vec{z}, a) \cdot \vec{R}(\vec{y}, b) \cdot \vec{R}(\vec{x}, c) \), where the matrices \( \vec{R}(\vec{z}, a) \), \( \vec{R}(\vec{y}, b) \), and \( \vec{R}(\vec{x}, c) \) are in the form (3); \( a, b, \) and \( c \) are the corresponding Euler angles. We note that the determination of Euler angles \( a, b \), and \( c \) is not unique (see [7]). The matrix of rotation \( \vec{Q} \) defined by the relation (9) can be decomposed into the product of the orthogonal matrices.

\[
\vec{Q} = \vec{R}(\vec{z}, a) \cdot \vec{R}(\vec{y}, b) \cdot \vec{R}(\vec{x}, c)
\]

By multiplying the left and right sides from the left of the matrix \( \vec{R}(\vec{z}, a) \) because the matrix \( \vec{R}(\vec{z}, a) \) is orthogonal \( \vec{R}(\vec{z}, a)^{-1} = \vec{R}(\vec{z}, a) \) and comparing suitably selected corresponding elements from the resulting matrix on the left and right sides of equation (8) modified in this way, we can determine the rotation angles \( a, b, \) and \( c \) (see [4], pp. 32). When calculating the angles of rotations, we use the \( \text{ATAN} \) function (part of the library of most programming languages), which calculates from the two input parameters \( \text{arg} \), and \( \text{arg} \), the value of the function \( \text{arctangent} \) for argument \( \text{arg} / \text{arg} \). Moreover, the signs of both input parameters are used to determine the quadrant in which the resulting value function is located (it is valid that \( -\pi < \text{ATAN}(\text{arg}, \text{arg}) < \pi \) part). We write the matrix of rotation \( \vec{Q} \) in the form by (10).

\[
\vec{Q} = \begin{bmatrix}
q_{11}(i) & q_{12}(i) & q_{13}(i) & 0 \\
q_{21}(i) & q_{22}(i) & q_{23}(i) & 0 \\
q_{31}(i) & q_{32}(i) & q_{33}(i) & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}
\]

Using the procedure described above for comparing the corresponding elements of the matrices in the modified equation (9) it is possible to obtain (11).

\[
a_i = \text{ATAN}2\left(\frac{q_{31}(i), q_{32}(i)}{q_{33}(i)}\right),
b_i = \text{ATAN}2\left(-\frac{q_{31}(i), q_{31}(i)\cos a_i + q_{32}(i)}{i \sin a_i}\right),
c_i = \text{ATAN}2\left(q_{31}(i)\sin a_i - q_{32}(i)\cos a_i\right)
\]
Thus, we determined rotation angles \( a_i, b_i, c_i \) in the equation (9) and the corresponding \( TCP_i \), defining the position and orientation of the LCS of the robot-end-effector in relation to the BCS of the robot. The \( TCP_i \) can be expressed in the form (12).

\[
TCP_i = (x_{aoi}, y_{alo}, z_{aoi}, a_i, b_i, c_i)
\]

(12)

where the elements of the vector \( u(i)_{BCS} \) are given by the relation (7).

3. Results and discussion

We focus on the practical problem of the passage of the non-bearing polyurethane frame with a circular cross-section through the fibre-processing head. The central 2D axis \( o \) of the frame is composed of two interconnected perpendicular arms (see Fig. 4). The axis \( o \) is entered into the LCS of the robot-end-effector using a discrete set of points \( B[i]_{LCS} \) \( 1 \leq i \leq N = 105 \). The total length \( d \) of the axis \( o \) from the starting point \( B[1]_{LCS} \) to the end point \( B[N]_{LCS} \) of the axis is \( d = 1050 \). The continuous distance of the points \( B[i]_{LCS} \) on the axis \( o \) from the starting point is denoted by the variable \( l \). The distance between two consecutive points \( B[i]_{LCS} \) and \( B[i+1]_{LCS} \) is \( h = 10 \text{mm} \). Vectors \( \text{vector 1}[1]_{LCS} \) and \( \text{vector 2}[1]_{LCS} \) are specified, radius of the frame is \( r_{CIRCLE} = 20 \text{ mm} \). The fibre-processing head is represented by the circles \( k_1 \) and \( k_2 \) with the centres \( S_1_{BCS} = [-1000,1105,990] \) and \( S_2_{BCS} = [-1000,1035,990] \) having the same radius \( r_{CIRCLE} = 40 \text{MM} \). The length of abscissa \( S_1_{BCS} \) \( S_2_{BCS} = 70 \text{mm} \). It is valid \( H_{BCS} = (S_1_{BCS} + S_2_{BCS})/2 \), \( \text{vector 1}[1]_{BCS} = (S_1_{BCS} - S_2_{BCS})/2 \), \( \text{vector 2}[1]_{BCS} = (0,0,1) \). The frame needs to be rotated at a distance of \( 550 \text{mm} \) from the beginning of the axis \( o \) to the distance of \( 690 \text{mm} \) around a tangent to the frame of axis \( o \) during the passing of point \( B[i]_{BCS} \) (for \( 56 \leq i \leq 69 \)) by point \( H_{BCS} \) when placing the longitudinal fibres relative to the axis \( o \) of the frame. This is a uniform right-handed rotary motion with an overall rotation angle \( \Theta = \pi \). The rotation is performed during the passage of the bent portion of the frame through the fibre-processing head. The calculation of the trajectory of the robot-end-effector from numerical model referred to in the previous chapter was applied to the described problem. Fig. 6 shows the position of the robot-end-effector when passing the polyurethane frame through winding head. Part a) shows the position of the robot-end-effector (first three parameters of \( TCP \)) and part b) the orientation of the robot-end-effector (last three parameters of \( TCP \)). Figures 7 and 8 compare the numerical model and the real experiment and illustrate the individually calculated values of \( TCP \) during the passing of the frame through the fibre-processing head. The comparison of an ideal sample and real sample from winding processing is seen in Fig. 9. Our article solves problem in which a composite frame with a circular cross-section is attached to
the end-effector of the industrial robot and successively passes through the fibre-processing head during the winding process. It is a similar problem as in [1 and 7]. We don’t know any other robotic workplace where similar technical problem production of composite with frame shape (the frame could be closed) is solved. This is the main problem to compare effectiveness of approach...
fibre winding technology on a open and closed non-bearing frame. This provides a significant advantage over users of the extended teach-in principle. The determination of the trajectory of the robot-end-effector using the given method can be used for optimising the trajectory of the robot-end-effector, too. Evolutionary optimising algorithms, in particular genetic algorithms or differential algorithms are often used in solving technical problems (see e.g. [6 - 8]). The described algorithm trajectory calculation can be applied to any manufacturing process where it is necessary to determine the 3D trajectory of a robot-end-effector. Suppliers of industrial robots currently offer specific software tools facilitating control of the robot-end-effector when programming specific tasks (e.g. welding, pressing, laser cutting, grinding). However, none of them are suitable to solve a technical problem of composite production and other general tasks related to the use of industrial robots. The procedure for determining the trajectory of the robot-end-effector is completely independent on the type of industrial robot and software tools. The procedure for determining the trajectory of the robot-end-effector induces virtually no additional costs to the manufacturer and can significantly speed up the determination of the desired trajectory of the robot-end-effector.

4. Conclusion

The described mathematical or numerical model with algorithm allows the accurate calculation and determination of the 3D trajectory of the robot-end-effector of the industry robot during the production of composite profile using the dry fibre winding technology on a open and closed non-bearing frame. This provides a significant advantage over users of the extended teach-in principle. The determination of the trajectory of the robot-end-effector using the given method can be used for optimising the trajectory of the robot-end-effector, too. Evolutionary optimising algorithms, in particular genetic algorithms or differential algorithms are often used in solving technical problems (see e.g. [6 - 8]). The described algorithm trajectory calculation can be applied to any manufacturing process where it is necessary to determine the 3D trajectory of a robot-end-effector. Suppliers of industrial robots currently offer specific software tools facilitating control of the robot-end-effector when programming specific tasks (e.g. welding, pressing, laser cutting, grinding). However, none of them are suitable to solve a technical problem of composite production and other general tasks related to the use of industrial robots. The use of the described algorithm is completely independent on the type of industrial robot and software tools. The procedure for determining the trajectory of the robot-end-effector induces virtually no additional costs to the manufacturer and can significantly speed up the determination of the desired trajectory of the robot-end-effector.

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References


